

# Time inconsistency and non-stationary instantaneous utility: empirical evidence from rural Malawi

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# Outline

- 1 Limits of the DU framework
- 2 Dynamic preferences update
- 3 Characterisation of the  $\beta$ -transformation
- 4 The resilience parameter
- 5 Comparative statics
- 6 Evolution of the EIS

# Empirical evidence of time inconsistency

- Which option do you prefer?
  - A) £100 today
  - B) £110 next week
- Which option do you prefer?
  - C) £100 one year from now
  - D) £110 one year and a week from now

Most people choose  $A \succ B$  and  $D \succ C$ , providing evidence of **time inconsistency**: a person's relative preference for well-being at an earlier date over a later date changes according to when she is asked.

This behaviour has been consistently detected in humans, rats and pigeons. (Ainslie, 1974)

- Time inconsistency is a puzzling result as it is in contrast with the predictions of the **discounted utility framework**<sup>1</sup> (DU).
- Most of the DU assumptions are very restricting and have been deeply falsified by empirical evidence.
- Nevertheless, the model is still very popular because of its simplicity, elegance and tractability.

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<sup>1</sup>Samuelson, Paul A. "A note on measurement of utility." The review of economic studies 4.2 (1937): 155-161.

# DU framework in a nutshell

- Consider an economy that lasts  $t = 1, \dots, T$  periods.
- The decision maker has preferences over consumption profiles  $c_t = (c_{t,t}, c_{t+1,t}, \dots, c_{T,t})$ , where  $c_{t,s}$  denotes the level of consumption in period  $t$  from period  $s$ ' perspective, with  $s, t \in \mathcal{T} = \{1, \dots, T\}$ .
- The agent has an initial endowment  $s_0$ .
- Postponing consumption to the next period gives a net return  $r > 0$ .

# DU framework in a nutshell

- Under completeness, transitivity and continuity the preferences over consumption profiles can be represented by an intertemporal utility function:

$$U^t(c_t, \dots, c_T) = \sum_{k=0}^{T-t} \delta^k u(c_{t+k})$$

- At each period  $t$ , the player chooses the optimal consumption profile  $c_t^* = (c_{t,t}^*, c_{t+1,t}^*, \dots, c_{T,t}^*)$  by maximising her intertemporal utility function.
- The initial optimal consumption plan is optimal for all the subsequent periods:  $c_{t,s}^* = c_{t,t}^* \forall s, t \in \mathcal{T}$ .

# Intertemporal choice and DU model

DU model is based on the following set of assumptions:

- 1 Integration of new alternatives with existing plans
- 2 Utility independence
- 3 Consumption independence
- 4 Stationary instantaneous utility
- 5 Independence of discounting from consumption
- 6 Constant discounting and time consistency
- 7 Diminishing marginal utility and positive time preference

Almost each assumption is usually violated by the empirical evidence:

- ① Limited ability of intertemporal reoptimization
- ② Habit formation
- ③ Preference for spread
- ④ State-dependent preferences
- ⑤ Labeled discount factors
- ⑥ Time inconsistency and present bias



- Literature usually explains time inconsistency by relaxing the DU assumption of constant discounting in favour of hyperbolic discounting: a person has a declining rate of time preferences.
- This idea has both sociological and psychological justifications.
- The most famous model of hyperbolic discounting is the  $(\beta, \delta)^2$ .
- However, it is unclear why the psychological motives should modify the discount factor rather than the utility function.
- The same phenomenon (and maybe more) can be explained by relaxing the assumption of stationary instantaneous utility.

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<sup>2</sup>Laibson, David. "Self-control and saving." Massachusetts Institute of Technology mimeo (1994).

# Advantages of the setting

Relaxing the assumption of stationary instantaneous utility rather than constant discounting provides several advantages:

- 1 Economic interpretation of fluctuations of the instantaneous utility is more intuitive.
- 2 Future-biased behavior becomes plausible.
- 3 Existence of a symmetric application to state-dependent preferences rather than time-dependent.

# Alternatives to the DU framework

- **Standard DU model:**

$$U^t(c_t, \dots, c_T) = \sum_{k=0}^{T-t} \delta^k u(c_{t+k})$$

- **$(\beta, \delta)$ -preferences:**

$$U^t(c_t, \dots, c_T) = u(c_t) + \beta \sum_{k=t+1}^T \delta^k u(c_k)$$

- **Dynamic utility:**

$$U^t(c_t, \dots, c_T) = \sum_{k=0}^{T-t} \delta^k u_t(c_{t+k})$$

# Dynamic preferences' update

- My model provides an alternative set-up to deal with time inconsistency by relaxing the assumption of stationary instantaneous utility.
- The novelty consists in the introduction of **law of motion** for the utility function relying on this semi-parametric assumption:

$$U^t(c_t, \dots, c_T) = \sum_{k=0}^{T-t} \delta^k [u(c_{t+k})]^{\beta_t}$$

- The semi-parametric approach allows to understand the main intuition of the phenomenon with a minimal divergence from the DU framework.
- All the other assumptions of the DU framework are retained.

# The concavifying parameter

- $\beta_t$  is an **unexpected** shock to the player's elasticity of intertemporal substitution at time  $t$ .
- The agent is **naive**: at any period,  $E_t(\beta_t) = 1$ .
- We remain agnostic on the reasons why  $\beta_t$  arises.
- $\beta_t$  has the following law of motion:

$$\beta_t = \begin{cases} 1 & \text{if } t = 1 \\ x_t & \text{if } t > 1 \end{cases}$$

$$x_t = \begin{cases} \beta_t^H \geq 1 & \text{w.p. } \theta \\ 0 < \beta_t^L < 1 & \text{w.p. } (1 - \theta) \end{cases}$$

with  $\theta \in [0, 1]$ . Draws are independent over time.

# Characterisation of the $\beta$ -transformation

Let us consider the following items:

- a consumption set  $C \subseteq \mathbb{R}_+$
- a  $C^2$  utility function  $u : C \rightarrow \mathbb{R}_+$ , with  $u'(c) \geq 0$  and  $u''(c) \leq 0$
- a real number  $\beta > 0$
- a function  $v : C \times \mathbb{R} \rightarrow \mathbb{R} : v(c, \beta) = u(c)^\beta$ .

Some restrictions on  $\beta$  must be imposed so that  $v(c)$  still represents convex preferences. In particular, the following is true:

## Proposition 1

*The maximum shock each agent can tolerate while retaining convex preferences is measured by the **resilience parameter**  $\tilde{\beta} = 1 - \frac{u''(c) \cdot u(c)}{u'(c)^2}$ .*

# Characterisation of the $\beta$ -transformation

Proof.

Consider  $v(c) = u(c)^\beta$ . This function represents convex preferences iff  $v''(c) \leq 0$ :

$$v''(c) = \beta u(c)^{\beta-1} \cdot \left[ u''(c) + (\beta - 1) \frac{u'(c)^2}{u(c)} \right] \leq 0$$

$$\Rightarrow \beta \in (0, \tilde{\beta})$$

where  $\tilde{\beta} = 1 - \frac{u''(c) \cdot u(c)}{u'(c)^2}$ .



# The resilience parameter

- $\tilde{\beta}$  depends on both the value of  $c$  and the shape of  $u$ . People can have different values of  $\tilde{\beta}$  because either their preferences are represented by different utility functions or because they have the same utility function but made different choices.
- the larger the interval  $(1, \tilde{\beta})$ , the more likely the individual is to retain convex preferences after a big shock. When making a choice of  $c$  under  $u$ , the decision maker implicitly determines the maximum shock she can tolerate while keeping standard behaviour.
- Since  $\tilde{\beta}$  depends on  $c$ ,  $\tilde{\beta}$  will generally be time-dependent in the intertemporal choice framework.



# The resilience parameter

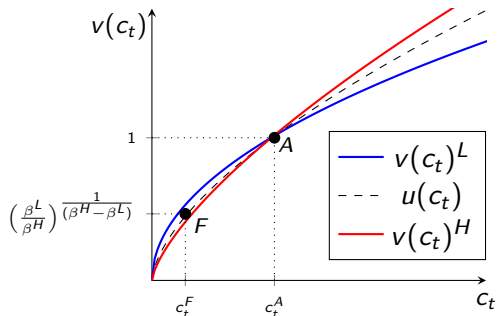
Focus on the second term of  $\tilde{\beta}$ :

$$\frac{u''(c) \cdot u(c)}{u'(c)^2} = \frac{u''(c)}{u'(c)} \cdot \frac{u(c)}{u'(c)}$$

- $\frac{u''(c)}{u'(c)} = \frac{d \log(u'(c))}{dc}$ : percentage change in marginal utility
- $\frac{u'(c)}{u(c)} = \frac{d \log(u(c))}{dc}$ : percentage change in level utility

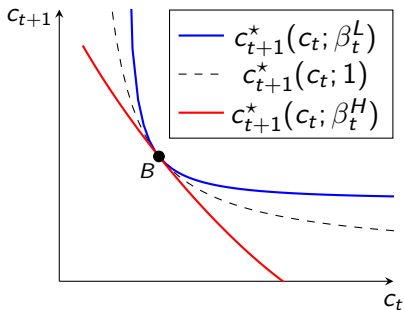
The term measures the **elasticity of the marginal utility with respect to the level utility**. So, it evaluates how much the power transformation can bend the utility function before making it linear.

# Comparative statics



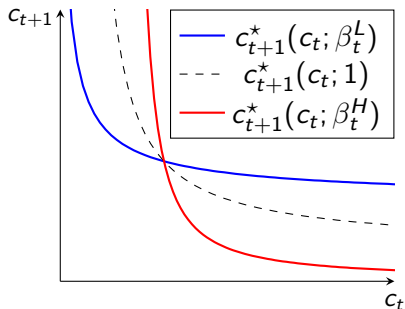
- The value functions are both increasing, and they cross at the point  $c_t^A$  s.t.  $u(c_t^A) = 1$
- $v^H$  is steeper than  $v^L$  as long as  $u(c_t) \geq \left(\frac{\beta^L}{\beta^H}\right)^{\frac{1}{\beta^H - \beta^L}}$
- $v^L$  is unambiguously more concave than  $v^H$ , which becomes convex if  $\beta^H \geq \tilde{\beta}$

# The bending effect



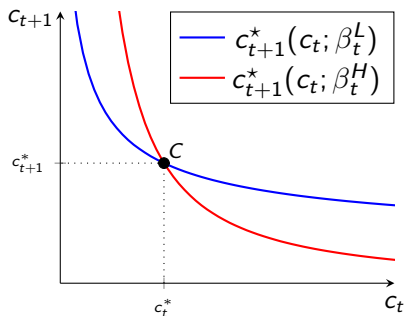
- If  $\beta_t < 1$  ( $\beta_t > 1$ ), the indifference curve becomes unambiguously **more** (less) **eccentric**.
- As the EIS increases (decreases), the agent requires weakly less (more) future consumption — given the same level of current consumption — in order to stick on the same utility level.
- If  $\beta_t \geq \tilde{\beta}_t$ , the indifference curve becomes concave.

# The tilting effect



- If  $\beta_t < 1$  ( $\beta_t > 1$ ), the indifference curve is **tilted to the left** (right).
- The net effect of the change in EIS depends on the level of current consumption.
- If  $\beta_t < 1$  ( $\beta_t > 1$ ), the change in future consumption required to stay on the same utility level is higher (lower) for small (high) amounts of current consumption.

# Single-crossing condition



**Single-crossing condition** for time-dependent indifference curves:

$$\left| \frac{\partial c_{t+1}}{\partial c_t} \Big|_{\beta_t \geq 1} \right| > \left| \frac{\partial c_{t+1}}{\partial c_t} \Big|_{\beta_t < 1} \right|$$

with  $\lim_{c_t \rightarrow 0} [c_{t+1}^*(c_t; \beta_t^H) - c_{t+1}^*(c_t; \beta_t^L)] \geq 0$

# Dynamic optimality conditions

At each period  $t$ , optimality requires:

$$\left[ \frac{u(c_{t+k})}{u(c_t)} \right]^{(\beta_t-1)} \cdot \frac{u'(c_{t+k})}{u'(c_t)} = [\delta(1+r)]^k \quad (1)$$

- The marginal rate of substitution at time  $t$  of consumption in any two periods depends on the realisation of  $\beta_t$ .
- It might be optimal to revise the consumption plan at each period.
- Crucially, this could lead to present-biased behaviour as well as feature-biased.

# Evolution of the EIS

- We expect the  $\beta$ -transformation to modify the elasticity of intertemporal substitution (EIS), which we denote as  $\gamma(c_t; \beta_t)$ .
- $\gamma(c_1; 1) = \gamma_1$  denotes the EIS at  $t = 1$ , *before* any  $\beta$ -transformation.
- $\gamma(c_t; \beta_t) = \gamma_t$  with  $t \neq 1$  denotes the EIS of the instantaneous utility at time  $t$  *after* the transformation.
- Our goal is to study the behaviour of  $\gamma_t$  assuming  $\beta_t \in (0, \tilde{\beta}_t)$ .

# Evolution of the EIS

- The abstract definition of elasticity of intertemporal substitution<sup>3</sup> is:

$$\gamma_v = -\frac{v'(c)}{c \cdot v''(c)} \quad (2)$$

where  $v'(c)$  and  $v''(c)$  denote the first and the second order derivative of  $v$  evaluated at point  $c$ , respectively.

- Since  $v(c, \beta) = u(c)^\beta$ , (2) is equivalent to:

$$\gamma_v = -\frac{u'(c)}{c \left[ u''(c) + (\beta - 1) \cdot \frac{u'(c)^2}{u(c)} \right]} \quad (3)$$

- Notice that  $\beta < \tilde{\beta} \Rightarrow \gamma_v \geq 0$  and  $\lim_{\beta \rightarrow \tilde{\beta}} \gamma_v = \infty$ .

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<sup>3</sup>Hall, Robert E. "Intertemporal Substitution in Consumption." *Journal of Political Economy* 96, no. 2 (1988): 339–57.



# Evolution of the EIS

## Proposition 2

Assume  $v(c) = u(c)^\beta$  and  $\beta \in (0, \hat{\beta})$ . Then  $\gamma(c, \beta)$  is increasing in  $\beta$ .

## Proof.

We want to show that for any pair  $(\beta_1, \beta_2)$  and for any  $c \in C$ ,  $\beta_1 < \beta_2 \Rightarrow \gamma(c, \beta_1) \leq \gamma(c, \beta_2)$ . Let us assume by contradiction this is not the case:  $\exists c \in C$  and a pair  $(\beta_1, \beta_2)$  with  $\beta_1 < \beta_2$  such that  $\gamma(c, \beta_1) > \gamma(c, \beta_2)$ . From Equation (3), this means:

$$-\frac{u'(c)}{c[u''(c) + (\beta_1 - 1) \cdot \frac{u'(c)^2}{u(c)}]} > -\frac{u'(c)}{c[u''(c) + (\beta_2 - 1) \cdot \frac{u'(c)^2}{u(c)}]} \quad (4)$$

Using the fact that  $\beta_1 \in (0, \hat{\beta})$  and  $\beta_2 \in (0, \hat{\beta})$ , Equation (4) simplifies to  $\beta_1 > \beta_2$ , contradicting our initial statement.  $\square$

# Application to CRRA

Assume  $u(c) = \frac{c^{(1-\sigma)}}{1-\sigma}$ , with  $\sigma \in (0, 1)$ .

Then, the following results:

- 1  $\tilde{\beta}_t = \tilde{\beta} = \frac{1}{1-\sigma}$
- 2  $\gamma_t = (1 + \sigma\beta_t - \beta_t)$
- 3  $u(c_t)^{\beta_t} = \left[ \frac{c_t^{(1-\sigma)}}{1-\sigma} \right]^{\beta_t} = \frac{\beta_t}{(1-\sigma)^{(\beta_t-1)}} \frac{c_t^{(1-\gamma_t)}}{1-\gamma_t}$

# Summary

- 1 Non-stationary instantaneous utility leads to different optimal solutions with respect to the theoretical benchmark.
- 2 Optimality usually requires a repeated revision of the consumption plan.
- 3 At each period  $t$ , the decision maker implicitly defines her resilience parameter, which is only partially determined by her intrinsic baseline preferences.
- 4 The net effect of a shock to the EIS can be split in a bending effect and a tilting effect.
- 5 According to the realisation of the shock, the revised optimal plan could either increase or decrease current consumption, explaining both present-biased and future-biased behavior.

## Empirical results

# Estimated parameters

- **Probability to get an high shock:**  $\hat{\theta} = 0.5$
- **Discount factor:**  $\hat{\delta} = 0.89$
- **EIS reciprocal:**  $\hat{\sigma} = 0.45$
- **Average beta:**  $\hat{\beta} = 1.34$
- **Average high beta:**  $\hat{\beta}^H = 2.04$
- **Average low beta:**  $\hat{\beta}^L = 0.66$
  
- Time-inconsistent plans: 93%
- Present-biased revisions: 30.5% <sup>4</sup>
- Future-biased revisions: 36.7% <sup>5</sup>

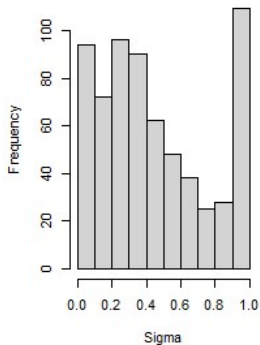
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<sup>4</sup>At least 3 present-biased revisions out of 5.

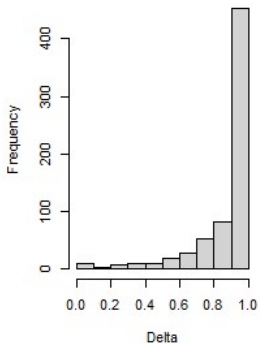
<sup>5</sup>At least 3 future-biased revisions out of 5.

# Estimated parameters

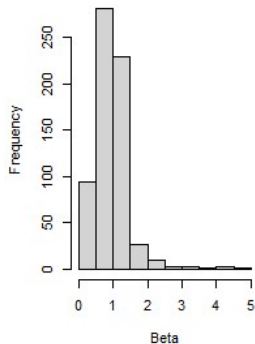
Estimated sigma



Estimated delta

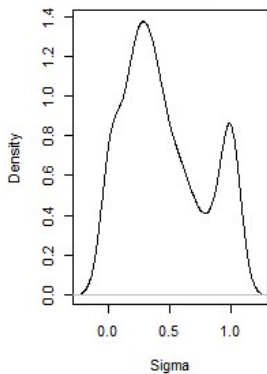


Estimated beta

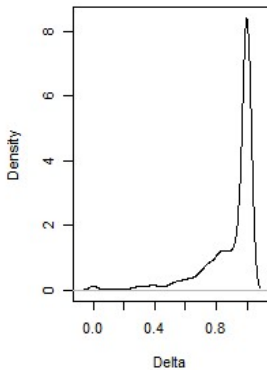


# Estimated parameters

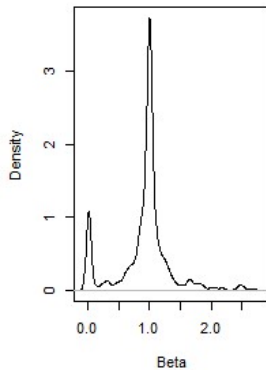
Estimated sigma



Estimated delta



Estimated beta



	$\delta$	$\frac{1}{\sigma}$	$\beta$
$\delta$	1	0.162	0.003
$\frac{1}{\sigma}$	0.162	1	-0.034
$\beta$	0.003	-0.034	1

Table: Correlation matrix

- The analysis reveals a slight positive correlation between the discount rate and the elasticity of intertemporal substitution.
- The result is in line with economic intuition: the higher is the elasticity of intertemporal substitution, the higher the weight the agent assigns to future periods.
- There is no empirical evidence of meaningful correlation between the other parameters of interests.



# Correlations

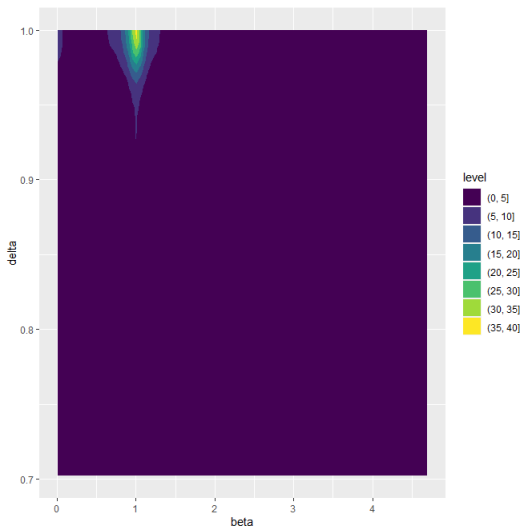


Figure: Contours of kernel density estimation of  $(\beta, \delta)$

# Correlations

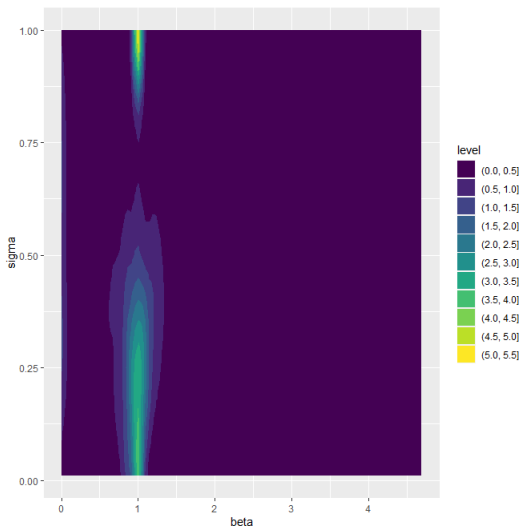


Figure: Contours of kernel density estimation of  $(\beta, \sigma)$

# Correlations

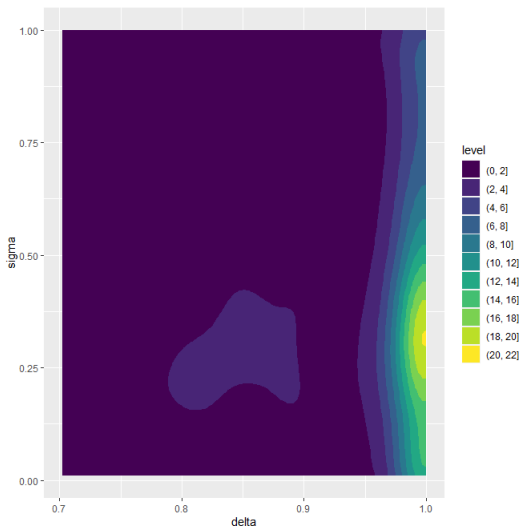
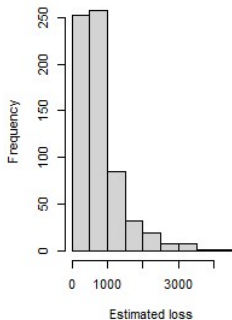


Figure: Contours of kernel density estimation of  $(\delta, \sigma)$

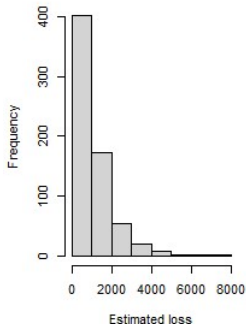
# Loss functions

Loss from model 1



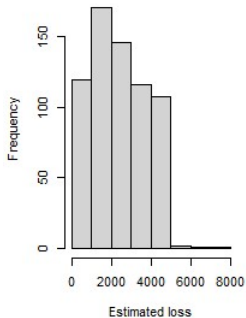
(a) Loss of model 1 for period 1

Loss from model 2



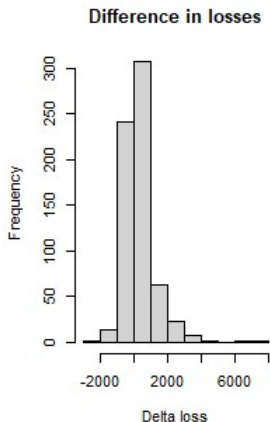
(b) Loss of model 2 for period 2

Alternative loss of revised plan

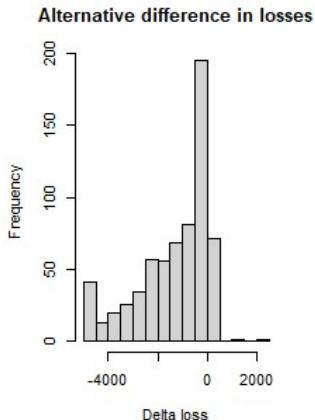


(c) Loss of model 1 for period 2

# Loss functions



(a) Difference in loss between model 2 for period 2 and model 1 for period 1



(b) Difference in loss between model 2 for period 2 and model 1 for period 2

# Model validation

Call:

```
lm(formula = loss.1 ~ male + younger + older + +no_school + some_primary +  
  primary + wealth_bline + r + wrdrecal_1 + ravens + finlit_total +  
  deathinfam + delta_income + delta_hh_tot_exp, data = mydataset)
```

Residuals:

Min	1Q	Median	3Q	Max
-936.2	-397.5	-104.3	203.8	3206.8

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	853.24403	159.26276	5.357	0.000000117 ***
male	-49.77443	55.11703	-0.903	0.367
younger	11.64881	61.42851	0.190	0.850
older	-15.83188	64.94493	-0.244	0.807
no_school	-48.73703	123.22783	-0.396	0.693
some_primary	-39.83558	101.69344	-0.392	0.695
primary	162.64959	111.39240	1.460	0.145
wealth_bline	-0.12404	0.11993	-1.034	0.301
r	66.46479	76.97005	0.864	0.388
wrdrecal_1	-11.72663	19.79709	-0.592	0.554
ravens	-5.83692	29.16114	-0.200	0.841
finlit_total	-47.84181	30.01856	-1.594	0.111
deathinfam	-80.38727	165.02896	-0.487	0.626
delta_income	0.01773	0.03515	0.504	0.614
delta_hh_tot_exp	0.01178	0.02147	0.549	0.583

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 625.9 on 647 degrees of freedom

Multiple R-squared: 0.01855, Adjusted R-squared: -0.002685

F-statistic: 0.8736 on 14 and 647 DF, p-value: 0.588

# Model validation

Call:

```
lm(formula = loss.1 ~ male + younger + older + +no_school + some_primary +  
  morethan_primary + wealth_bline + r + wrdrecal_1 + ravens +  
  finlit_total + deathinfam + delta_income + delta_hh_tot_exp,  
  data = mydataset)
```

Residuals:

Min	1Q	Median	3Q	Max
-936.2	-397.5	-104.3	203.8	3206.8

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	1015.89361	139.12597	7.302	0.0000000000000836 ***
male	-49.77443	55.11703	-0.903	0.36683
younger	11.64881	61.42851	0.190	0.84966
older	-15.83188	64.94493	-0.244	0.80748
no_school	-211.38662	97.98723	-2.157	0.03135 *
some_primary	-202.48517	75.35626	-2.687	0.00739 **
morethan_primary	-162.64959	111.39240	-1.460	0.14473
wealth_bline	-0.12404	0.11993	-1.034	0.30140
r	66.46479	76.97005	0.864	0.38817
wrdrecal_1	-11.72663	19.79709	-0.592	0.55383
ravens	-5.83692	29.16114	-0.200	0.84142
finlit_total	-47.84181	30.01856	-1.594	0.11148
deathinfam	-80.38727	165.02896	-0.487	0.62635
delta_income	0.01773	0.03515	0.504	0.61416
delta_hh_tot_exp	0.01178	0.02147	0.549	0.58333

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```
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    delta_hh_tot_exp, data = mydataset)
```

Residuals:

```
    Min       1Q   Median       3Q      Max
-821.2 -397.8 -108.4  216.5 3207.5
```

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	767.952359	113.463606	6.768	0.0000000000292 ***
male	-29.579962	54.809698	-0.540	0.590
younger	6.865915	59.543494	0.115	0.908
older	-16.593211	65.207823	-0.254	0.799
yesed	32.798769	72.290848	0.454	0.650
wealth_bline	-0.093468	0.119854	-0.780	0.436
r	64.954027	77.040916	0.843	0.399
wrdrecal_1	-7.507623	19.812652	-0.379	0.705
ravens	-2.232835	28.874697	-0.077	0.938
finlit_total	-30.132138	28.739543	-1.048	0.295
deathinfam	-66.821465	165.621278	-0.403	0.687
delta_income	0.028229	0.035058	0.805	0.421
delta_hh_tot_exp	0.006995	0.021479	0.326	0.745

```
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 628.4 on 649 degrees of freedom

Multiple R-squared: 0.007505, Adjusted R-squared: -0.01085

F-statistic: 0.409 on 12 and 649 DF, p-value: 0.9604



# Model validation

Call:

```
lm(formula = loss.2 ~ male + younger + older + no_school + some_primary +  
  primary + wealth_bline + r + wrdrecal_1 + ravens + finlit_total +  
  deathinfam + delta_income + delta_hh_tot_exp, data = mydataset)
```

Residuals:

Min	1Q	Median	3Q	Max
-1203.2	-589.8	-258.2	287.9	6232.7

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	1298.775787	248.322979	5.230	0.000000229 ***
male	37.912260	85.938636	0.441	0.659
younger	40.119712	95.779517	0.419	0.675
older	-75.445487	101.262331	-0.745	0.457
no_school	-175.811585	192.137200	-0.915	0.361
some_primary	-87.846620	158.560709	-0.554	0.580
primary	-32.208671	173.683366	-0.185	0.853
wealth_bline	0.026257	0.186999	0.140	0.888
r	-74.329607	120.011930	-0.619	0.536
wrdrecal_1	-22.134701	30.867680	-0.717	0.474
ravens	21.579117	45.468134	0.475	0.635
finlit_total	-28.843371	46.805034	-0.616	0.538
deathinfam	-378.258482	257.313653	-1.470	0.142
delta_income	-0.007301	0.054805	-0.133	0.894
delta_hh_tot_exp	-0.009073	0.033481	-0.271	0.786

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 975.9 on 647 degrees of freedom

Multiple R-squared: 0.009479, Adjusted R-squared: -0.01195

F-statistic: 0.4422 on 14 and 647 DF, p-value: 0.9607

# Model validation

```
Call:
lm(formula = loss.prime ~ male + younger + older + no_school +
    some_primary + primary + wealth_bline + r + wrdrecal_1 +
    ravens + finlit_total + deathinfam + delta_income + delta_hh_tot_exp,
    data = mydataset)
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-2912.6 -1047.8  -113.1   961.9  4973.0
```

```
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  1452.57156   336.20622    4.320 0.0000180 ***
male          197.05802   116.35292    1.694  0.0908 .
younger       23.98978   129.67656    0.185  0.8533
older        -140.02508   137.09978   -1.021  0.3075
no_school    -60.83833   260.13590   -0.234  0.8152
some_primary  31.92374   214.67645    0.149  0.8818
primary       18.44248   235.15112    0.078  0.9375
wealth_bline  0.38872     0.25318    1.535  0.1252
r             719.65828   162.48499    4.429 0.0000111 ***
wrdrecal_1    64.51807   41.79197    1.544  0.1231
ravens        -9.08247   61.55962   -0.148  0.8828
finlit_total  141.95013   63.36966    2.240  0.0254 *
deathinfam   -193.66705   348.37875   -0.556  0.5785
delta_income  0.01891     0.07420    0.255  0.7989
delta_hh_tot_exp 0.02589    0.04533    0.571  0.5681
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 1321 on 647 degrees of freedom
Multiple R-squared:  0.07094, Adjusted R-squared:  0.05083
F-statistic: 3.529 on 14 and 647 DF, p-value: 0.00001293
```

# Model validation

```
Call:
lm(formula = dloss21 ~ male + younger + older + no_school + some_primary +
    primary + wealth_bline + r + wrdrecal_1 + ravens + finlit_total +
    deathinfam + delta_income + delta_hh_tot_exp, data = mydataset)
```

Residuals:

Min	1Q	Median	3Q	Max
-2353.6	-431.2	-188.2	234.5	6857.2

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	445.53176	234.02879	1.904	0.0574
male	87.68669	80.99176	1.083	0.2794
younger	28.47090	90.26617	0.315	0.7526
older	-59.61361	95.43338	-0.625	0.5324
no_school	-127.07455	181.07723	-0.702	0.4831
some_primary	-48.01104	149.43350	-0.321	0.7481
primary	-194.85826	163.68565	-1.190	0.2343
wealth_bline	0.15030	0.17624	0.853	0.3941
r	-140.79440	113.10370	-1.245	0.2136
wrdrecal_1	-10.40807	29.09085	-0.358	0.7206
ravens	27.41603	42.85086	0.640	0.5225
finlit_total	18.99844	44.11080	0.431	0.6668
deathinfam	-297.87121	242.50194	-1.228	0.2198
delta_income	-0.02503	0.05165	-0.485	0.6281
delta_hh_tot_exp	-0.02086	0.03155	-0.661	0.5088

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 919.7 on 647 degrees of freedom  
Multiple R-squared: 0.01481, Adjusted R-squared: -0.006506  
F-statistic: 0.6948 on 14 and 647 DF, p-value: 0.7806

# Model validation

Call:

```
lm(formula = dloss2prime ~ male + younger + older + no_school +  
  some_primary + primary + wealth_bline + r + wrdrecal_1 +  
  ravens + finlit_total + deathinfam + delta_income + delta_hh_tot_exp,  
  data = mydataset)
```

Residuals:

Min	1Q	Median	3Q	Max
-3805.3	-748.9	348.1	1060.9	3749.2

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-153.79577	352.72983	-0.436	0.6630
male	-159.14576	122.07135	-1.304	0.1928
younger	16.12994	136.04980	0.119	0.9057
older	64.57960	143.83785	0.449	0.6536
no_school	-114.97325	272.92086	-0.421	0.6737
some_primary	-119.77036	225.22721	-0.532	0.5951
primary	-50.65115	246.70815	-0.205	0.8374
wealth_bline	-0.36246	0.26562	-1.365	0.1729
r	-793.98789	170.47068	-4.658	0.00000388 ***
wrdrecal_1	-86.65277	43.84593	-1.976	0.0485 *
ravens	30.66159	64.58511	0.475	0.6351
finlit_total	-170.79350	66.48411	-2.569	0.0104 *
deathinfam	-184.59144	365.50061	-0.505	0.6137
delta_income	-0.02621	0.07785	-0.337	0.7364
delta_hh_tot_exp	-0.03497	0.04756	-0.735	0.4625

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1386 on 647 degrees of freedom

Multiple R-squared: 0.06913, Adjusted R-squared: 0.04899

F-statistic: 3.432 on 14 and 647 DF, p-value: 0.00002091

- Baseline regressions on beta: <http://localhost:28709/session/viewhtml4c5c229272b1/index.html>
- Regressions including  $(\sigma, \delta)$ : <http://localhost:28709/session/viewhtml4c5c7e1b3bd3/index.html>

# Comparison with hyperbolic discounting

- It is possible to prove that there exists a perfect mapping between the non-stationary utility approach and non-constant discounting **if** we allow the discount factor to be increasing over time.
- The change in instantaneous utility can be indeed caused by a change in the value we assign to future.
- However, the model is agnostic on the topic and does not rule out other possible interpretations.

# Comparison with hyperbolic discounting

- One might ask if relaxing constant discounting rather than stationary instantaneous utility would provide better fit.
- Since there exists a perfect mapping between the two problems, the answer is no **if** we allow the discount factor to be increasing over time.
- In this case, the loss functions would be equal.
- If we want to restrict our focus on hyperbolic discounting — as the literature usually does — the loss in fit will increase.
- The advantage of the non-stationary instantaneous utility framework is that both downwards shocks and upwards ones are plausible.
- The underlying economic intuition is more convincing if applied to utility rather than to discount factors.